Exercises on Lie groups

Spring term 2018, Sheet 13

Hand in before 10 o'clock on 24th May 2018 Mail box of Sven Raum in MA B2 475 Sven Raum Gabriel Jean Favre

Exercise 1

Show that every connected abelian Lie group is of isomorphic with $\mathbb{R}^m \times \mathbb{T}^n$ for some $m, n \in \mathbb{N}$.

Exercise 2

Show that every connected simply connected solvable Lie group is contractible.

Exercise 3

Show that every Lie group is homotopic to a compact Lie group, making use of the Iwasawa decomposition of semi-simple Lie groups.